

Electronics III

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Course Outline

Models for Integrated-Circuit Active Devices

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Course Outline

- **MOS Transistor Models and physics**
- MOSFET and Junction FET
- MOS capacitor
- MOS threshold
- MOS regions (linear & saturation) characteristic
- Small-Signal Model
- Examples of small-signal Analysis
 - Transconductance Amp
 - Diode
 - Source Follower
- Capacitance
- Higher order models

References:
Razavi's IC Book, L&S

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Course Outline

- **Bipolar Transistor Models**
- Hybrid-small-signal model (for BJT)
 - model elements
 - Common-Emitter (current drive, voltage drive)
 - Common-Collector
 - Common - Base
 - Ohmic Resistance
- Lateral PNP transistors
- Other Components
 - Base diffusion resistor
 - Other resistor
 - Capacitor
 - Inductor

References:
Gray & Mayer's IC Book, L&S

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Course Outline

- **Single- Stage Amplifiers**
- Basic Concepts
- Common-Source Stage
 - Common-Source Stage with Resistive Load
 - CS Stage with Diode-Connected Load
 - CS Stage with Current-Source Load
 - CS Stage with Triode Load
 - CS Stage with Source Degeneration
- Source follower
- Common-Gate Stage
- Cascode stage
 - Folded Cascode
- Choice of Device Models

Reference:
Razavi's IC Book

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Course Outline

- **Differential Amplifiers**
- Single-Ended and Differential operation
- Basic Differential Pair
 - Qualitative Analysis
 - Quantitative Analysis
- Common mode Response
- Differential Pair with MOS Loads
- Gilbert Cell

Reference:
Razavi's IC Book

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Course Outline

- **Frequency Response of Integrated circuits**
- Single-Stage Amplifier frequency response
 - Differential Amp frequency response
 - Common-Mode (CM) gain in diff pair
 - Emitter-follower freq response
 - Common-Base freq response
- multistage Amp freq response
 - Dominant Pole Approximation
 - Zero-value Time constant Analysis
 - Common-Emitter cascade freq response
 - Cascode freq response

References:
Razavi,
Gray & Mayer's
IC Book

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Course Outline

- **Elementary Transistor stages**
- MOS single Transistor Amplifying stages
 - Biasing ,Gain ,Bandwidth , high frequency performance ,
 - Unity- Gain freq & GBW product
- Source & Emitter Followers
 - DC level shift ,high freq Gain ,Output Impedance
- Cascode Transistors
 - MOS cascode (Low freq Analysis ,high freq performance).
 - Bipolar cascode
- Cascode stages
 - BW of cascode w/ low and w/Active load ,High voltage cascode,
 - cascode w/Bipolar ,Feedforward in cascode Amp

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Course Outline

- **Differential Stage**
MOS differential stages (DC characteristic , small-signal behavior ,low freq analysis ,GBW product, Slew-rate)
- **Current mirrors**
Simple MOS current Mirror
Other current mirror
Bipolar current mirror
Gain factor mismatch
Body factor mismatch
Offset voltage
Mismatch effects on Current mirror
Differential stage w/ Active load
CMRR
Design for low offset and drift
Power Supply Rejection Ratio (PSRR)

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Course Outline

- **Design options :**
Design for optimum GBW or SR
Compensation of the Positive Zero

Reference: L&S

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Course Outline

- **Frequency Response stability of feedback Amplifiers**
- **The Stability Problem**

References:
Gray & Meyer IC book,
Sedra & Smith

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Course Outline

- **Operational Amplifier Design**
- **Design of a simple CMOS OTA**
Gain
GBW and Φ_M
- **Design plan : optimization for Maximum GBW**
- **The Miller CMOS OTA**
Operation
Gain
GBW and Φ_M
Design plan : Determine Compensation Cap Cc Determine size and I

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Course Outline

- Full set of characteristic of Miller OTA
 - CM input vs. supply
 - Output voltage range vs. Supply
 - Max output current (sink and source)
 - AC analysis :low freq.
 - GBW vs.. I_{BIAS}
 - Slew-rate vs. load cap
 - Output voltage range vs. Frequency
 - Settling time
 - Output Impedance
 - temperature effects
- Matching characteristics
 - transistor Mismatch model
 - Threshold voltage Mismatch V_T

**Reference:
L&S**

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Course Outline

- **And Special Issues**

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References

- *Design of Analog CMOS Integrated Circuit*, Behzad Razavi
McGraw-Hill 2001
- *Analysis and design of Analog Integrated Circuits*, Gray –
Hurst-Lewis- Mayer Forth Edition John Wiley & SONS,INC 2004
- *Design of Analog Integrated circuit & systems*, Kenneth R.
Laker, Willy M.C .Sansen .McGraw-Hill 1994
- *Microelectronic Circuit*, Adel S. Sedra , Kenneth C. Smith ,
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- *Analog Integrated Circuit Design* ,David A. Johns ,Ken Martin
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Grading

Assignment : 10%

Project : 20%

Quiz :10%

Mid term :20%

Final term :40%

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Field Effect Transistors (FET)

JFET: Junction FET

MOSFET(MOST): Metal-Oxide Semiconductor FET

Fig 1.1 a
n-channel JFET

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Field Effect Transistors (FET)

- Channel is sandwiched between two depletion layers which isolate channel from two conducting layer: Gate (p+ in n-channel) and substrate (p in n-channel).
- These depletion layers form junction capacitances between the channel to the top gate C_{gs} and to the bottom layer C_{bs} . The voltage across each capacitance controls the widths of the depletion layer and hence, the widths of the residual channel between both depletion layers. The voltage across C_{gs} and C_{bs} control the conductivity of the channel as well as its charge, so, the current. Either C_{gs} or C_{bs} can independently control the current through channel.

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Field Effect Transistors (FET)

Fig 1.1 b
p-channel JFET

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Field Effect Transistors (FET)

- The channel is isolated from the top gate G , by a depletion layer with width h . The channel is also isolated from the substrate or bulk B , by another depletion layer.
- Both depletion layers modulate the channel conductivity or pinch-off (no I_D current, $I_D = 0$ the channel entirely).
- This (pinch-off) can be done by reverse biasing the voltage across these depletion layers (respect to the source).
- Note usually the bulk is at a constant negative voltage or connected to source so only the top gate (like CMOS) is used to control the transistor current.
- The depletion layer of the top gate G can fully pinch off the channel, provided its thickness h is made equal to the thickness of the channel a_c .
- The voltage V_{GS} requested to fully pinch-off the channel (for zero V_{DS}) is called pinch-off voltage V_P .

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Field Effect Transistors (FET)

Consider a PN Junction (Fig 1.2)

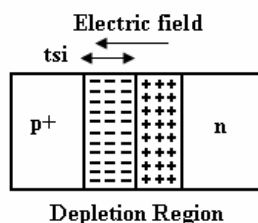


Fig 1.2
PN Junction

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Field Effect Transistors (FET)

- In the **p+** side a large number of free positive carriers are available, whereas in the **n** side, many free negative carriers are available.
- The hole, in the **p+** side tend to diffuse in to the **n** side, whereas the free electrons in the **n** side tend to diffuse to the **p+** side.
- This diffusion lowers the concentration of free carriers in the region between the two sides.
- As the two types of carriers diffuse together, they recombine. Every electron that diffuse from n-side to the p-side leaves behind a “**bound**” positive charge close to the transition region. Similarly, every hole that diffuse from the p-side leaves behind a bound electron near transition region.
- This diffusion of free carriers create a depletion region at the junction of the two sides where no free carriers exist.

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Field Effect Transistors (FET)

- The total amount of “bound” charge on the two sides of junction must be equal for charge neutrality.
- This requirement causes the depletion region to extend further into the more lightly doped n-side than into the p+ side.
- As these bound charges are exposed, an electric field develops going from the n-side to the p-side. This electric field is often called the built-in potential of the junction. It opposes the diffusion of free carriers until there is no movement of charge under open-circuit condition.

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Field Effect Transistors (FET)

Recall for a one-sided abrupt junction, the thickness of the depletion layer is:

$$t_{si} = \sqrt{\frac{2\epsilon_{si}(\Phi_j - V_{BC})}{qN_{SUB}}} \text{ or } (\Phi_j + V_R) \quad \text{Where } V_R = -V_{Bis} \text{ is the reverse bias voltage across p-n junction} \quad (1-1)$$

The layer reverse bias is the thicker depletion layer becomes

V_{BC} is the reverse bias voltage

Φ_j is the bulk-channel junction built-in voltage

$$\Phi_j = \frac{kT}{q} \ln \frac{N_c N_{SUB}}{n_i^2} \quad n_i = 1.5 \times 10^{10} / \text{cm}^3 @ 27^\circ \text{C} \quad (1-2)$$

Note that always $V_{SB} > 0$ for nmos

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Field Effect Transistors (FET)

Substituting V_{BC} by V_p and t_{si} by a_c :

$$V_p = \frac{qN_A a_c^2}{2\epsilon_{si}} - \Phi_j \quad \text{doping in p+ in channel} \quad (1-3)$$

This JFET is depletion type, meaning the conducting channel already exists for $V_{GS} = 0$ must be positive.

By means of Ion-implmentation technology, thinner channels ($< 0.2 \mu m$) can be realized

$$V_p = 1V \rightarrow a_c \approx 0.16 \mu m$$

$$V_p = 0V \rightarrow a_c \approx 0.11 \mu m$$

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Field Effect Transistors (FET)

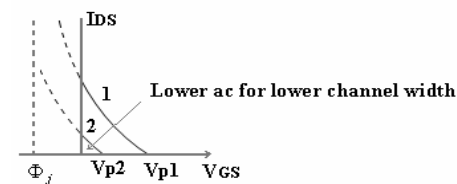


Fig 1.3

The forward bias V_{GS} are shown by dashed lines in Fig 1.3. Higher than the diode voltage large forward current starts to flow through gate. Forward bias gate must be avoided due to gate leakage current.

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MOST

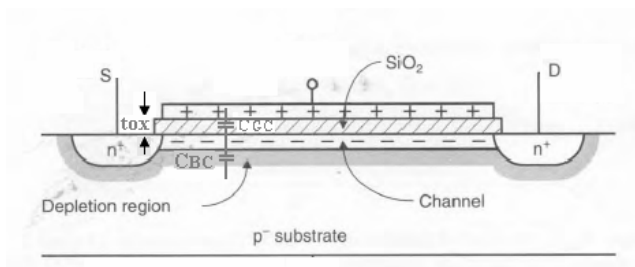


Fig 1.4 a
nMOST

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MOST

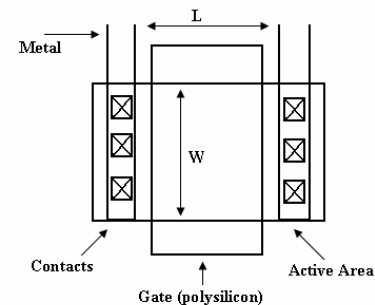


Fig 1.4 b
nMOST layout

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MOST

- Channel is sandwiched between an oxide layer and a depletion layer. These oxide and depletion layers isolate channel from two conductive layers (Gate) and (Substrate).
- These isolation layers again form caps: C_{GC} and C_{BC}
- C_{GC} is an oxide cap but C_{BC} is a depletion cap.
- Oxide cap is less efficient:

$$\epsilon_{ox} = 0.34 \text{ pF/Cm} \quad \epsilon_{si} = 1.06 \text{ pF/Cm}$$

$$\Rightarrow \epsilon_{si} \approx 3\epsilon_{ox}$$

MOST

- Oxide cap is independent of the applied voltage!
- The applied voltage on C_{GC} and C_{BC} control the charge in residual channel and so the current.
- Current establishes if $V_{GS} > V_{th}$ (threshold voltage) for $V_{DS} > 0$

MOST

- pmos and nmos need substrate material of opposite type

Fig 1.5
N-well CMOS technology

MOS Capacitance (Oxide)

$$C_{GC} = WLC_{ox} \quad C_{ox} = \frac{\epsilon_{ox}}{t_{ox}} \quad (1-4)$$

Examples:

For 0.25 μm technology $t_{ox} = 4\text{nm} = 40 \text{ \AA}$

$C_{ox} = 8.5 \text{ fF}/\mu\text{m}^2$ Very efficient capacitance

Very old technology $t_{ox} = 50\text{nm}$ $C_{ox} = 6.8 \times 10^{-8} \text{ F/Cm}^2 = 0.68 \text{ fF}/\mu\text{m}^2$
 $WL = (50 \times 5) \mu\text{m}^2 \Rightarrow C_{GC} = 0.17 \text{ pF} = 170 \text{ fF}$

For modern technologies: $C_{GC} = 2.125 \text{ pF} (WL = 250 \mu\text{m}^2)$

MOS Capacitance (Junction)

$$C_{BC} = WLC_j \quad C_j = \frac{\epsilon_{si}}{t_{si}} \quad (1-5)$$

Where t_{si} is the thickness of depletion layer between channel and bulk. t_{si} depends on the voltage across the depletion layer and on the doping level N_{SUB} of the substrate.

For and abrupt junction:

$$t_{si} = \sqrt{\frac{2\epsilon_{si}(\Phi_j - V_{BC})}{qN_{SUB}}} \quad \Phi_j = \frac{kT}{q} \ln \frac{N_c N_{SUB}}{n_i^2}$$

$$n_i = 1.5 \times 10^{10} / \text{cm}^3 @ 27^\circ\text{C}$$

Φ_j is the reverse bias voltage (some times referred to as Φ_0)
 V_{BC} is the bulk-channel junction built-in voltage

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MOS Capacitance (Junction)

Normally $V_{BC} = V_{BS}$ (channel and source potential the same at the source side)

Note: As $\Phi_F = \frac{kT}{q} \ln \frac{N_{SUB}}{n_i}$ if $N_C = N_{SUB} \Rightarrow \Phi_j = 2\Phi_F$

Note: $V_R \uparrow \Rightarrow t_{si} \uparrow \Rightarrow C_j \downarrow$

Note: $\Phi_j - V_{BC} = \Phi_j - V_B + V_{ch} \Rightarrow$

For $V_{ch} = V_D$ since $V_D > V_S$ (as in nmos p-sub is grounded so is more reversed biased) so is thicker in Drain side!

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MOS Capacitance (Junction)

for $N_{SUB} = 3 \times 10^{14} \text{ cm}^{-3}$ $n^+, N_C = 2 \times 10^{17} \text{ cm}^{-3}$:

$$\Phi_j = 0.68V \quad \text{Almost 1/10 of } C_{ox}$$

$$\text{for } V_{BS} = 0 : t_{si} = 1.73 \mu\text{m} \Rightarrow \begin{cases} C_j = 0.67 \times 10^{-8} \text{ F/cm}^2 \\ C_{BC} = 15 \text{ fF} \end{cases}$$

Note: The depletion layer thickness(1730 nm)>>Oxide thickness(50nm) so always:

$$C_{BC} \ll C_{GC}$$

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Model MOST-JFET

- MOST is actually a parallel connection of a MOST and a JFET (parasitic) which is usually common for all MOST (single substrate). note that JFET is always off*
- Gate control is seen as a MOST(CMOS) and the bulk control is regarded by JFET in this model!*
- The effect of parasitic JFET in a MOST is shown in value by γ (gamma) factor. This is so called body factor.*

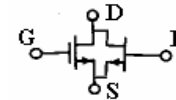


Fig 1.6
MOSFET-JFET Model

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Model MOST-JFET

$$\gamma = \frac{\sqrt{2\epsilon_{si}qN_{SUB}}}{C_{ox}} \quad V^{1/2} \text{ dimension} \quad (1-6)$$

By one of the expressions of C_{BC} and C_{GC} we can write:

$$\left\{ \begin{array}{l} C_{BC} = WLC_j = WL \frac{\epsilon_{si}}{\sqrt{\frac{2\epsilon_{si}(\Phi_j - V_{BS})}{qN_{SUB}}}} = WL \frac{\sqrt{\epsilon_{si}qN_{SUB}}}{\sqrt{2(\Phi_j - V_{BS})}} \\ C_{GC} = WLC_{ox} \end{array} \right.$$

$$\Rightarrow \frac{C_{BC}}{C_{GC}} = \frac{\sqrt{\epsilon_{si}qN_{SUB}}}{C_{ox}} \cdot \frac{1}{\sqrt{2(\Phi_j - V_{BS})}} = \frac{\sqrt{2\epsilon_{si}qN_{SUB}}}{C_{ox}} \cdot \frac{1}{2\sqrt{(\Phi_j - V_{BS})}}$$

$$\Rightarrow \gamma = \frac{C_{BC}}{C_{GC}} 2\sqrt{\Phi_j - V_{BS}} = \frac{C_{BC}}{C_{GC}} 2\sqrt{\Phi_j + V_{SB}} \quad (1-7)$$

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Model MOST-JFET

- The depletion charge Q_D contributing to threshold voltage is function of V_{BS} . This charge depends on the depletion thickness t_{si} as given by $Q_D = qN_{Bulk}t_{si}$ so:

$$\frac{Q_D}{C_{ox}} = \frac{qN_{Bulk}}{C_{ox}} \sqrt{\frac{2\epsilon_{si}(\Phi_j - V_{BS})}{qN_{Bulk}}} \leftarrow t_{si} \quad (1-8)$$

$$\therefore \frac{Q_D}{C_{ox}} = \frac{\sqrt{2qN_{Bulk}\epsilon_{si}}}{C_{ox}} \sqrt{2|\Phi_F| - V_{BS}} \quad * \quad (1-9)$$

- The minimum voltage needed on surface to push down the depletion region is $\Phi_j = 2|\Phi_F|$ or the voltage to just create mobile electrons (charges).

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Model MOST-JFET

- equation(*) for 1) $V_{BS} = 0$ $\frac{Q_D}{C_{ox}} = \gamma\sqrt{2|\Phi_F|}$
2) $V_{BS} < 0$ $\frac{Q_D}{C_{ox}} = \gamma\sqrt{2|\Phi_F| - V_{BS}}$

so defining V_{T0} for $V_{BS} = 0$ when $V_{BS} = 0$ is obvious that V_T greater than V_{T0} for $V_{BS} < 0$ as follows:

$$V_T = V_{T0} + \gamma(\sqrt{2|\Phi_F| - V_{BS}} - \sqrt{2|\Phi_F|}) \quad (1-10)$$

- In other words, say in NMOS, when $V_{BS} < 0$ source/channel voltage is higher respect to bulk there are positive charges on the top plate of C_{BC} (due to charge in depletion region). therefore in order to cancel these extra charges the more positive voltage than V_{T0} must be applied on top plate of C_{GC} that it's bottom plate (i.e. channel) produces more negative charges to account for depleted positive charges on the surface.

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Model MOST-JFET

- So body factor γ is directly proportional to the ratio of controlling caps C_{BC} and C_{GC} . The proportionality factor $\frac{C_{BC}}{C_{GC}}$ is the voltage dependence of the bulk junction capacitance $\frac{C_{BC}}{C_{GC}}$.

A Definition:

$$n - 1 = \frac{C_{BC}}{C_{GC}} = \frac{\gamma}{2\sqrt{\Phi_j - V_{BS}}} > 0 \quad (1-11)$$

Note: n depends on the applied voltage V_{BS} whereas γ does not. Parameters γ and n are the first two parameters of the MOST model that depends on N_{SUB} and ϵ_{si} values.

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Model MOST-JFET

Example:

For:

$$C_{ox} = 6.8 \times 10^{-8} \text{ F/cm}^2, n_{sub} = 3 \times 10^{14} \text{ cm}^{-3} \\ \Rightarrow \gamma = 0.15 \text{ V}^{1/2} \text{ for } V_{BS} = 0 \Rightarrow n = 1.09$$

But for:

$$n_{sub} = 10^{16} \text{ cm}^{-3} \Rightarrow \gamma = 0.86 \text{ V}^{1/2}, n = 1.49$$

Note: GAMMA (γ) is a constant SPICE model parameter not n . it is obvious that n is bias dependent.

MOST Threshold Voltage

V_{T0} is obtained from semiconductor physics for $V_{BS} := 0$

$$V_{T0} = \Phi_{GB} - \frac{Q_{ox}}{C_{ox}} + 2\Phi_F \pm \frac{Q_D}{C_{ox}} \quad (1-12)$$

With + for nMOST and – for pMOST. It is independent of the voltage applied.

MOST Threshold Voltage

V_{T0} terms:

- 1) Φ_{GB} is the difference in the work function between the gate material and the bulk material.
With n+ polysilicon with N_G doping for gate: for p-bulk doping of (nMOST): N_B

$$\Phi_{GB} = -\frac{kT}{q} \ln \frac{N_G N_B}{n_i^2} \quad \begin{matrix} N_B \approx [3 \times 10^{14} - 10^{16}] \text{ cm}^{-3} \\ N_G \approx 2 \times 10^{19} \text{ cm}^{-3} \end{matrix} \quad (1-13)$$

for a pMOST: for n-bulk doping N_B :

$$\Phi_{GB} = -\frac{kT}{q} \ln \frac{N_G}{N_B} \quad N_B \approx [3 \times 10^{14} - 10^{16}] \text{ cm}^{-3} \quad (1-14)$$

MOST Threshold Voltage

- 2) Charge Q_{ox} represents the positive charges (in C_{cm}) at the silicon-oxide interface. New technology tries to minimize them to avoid dV_{th} . In SPICE it represents by NSS .

Flat Band Voltage:

$$V_{FB} = \Phi_{GB} - \frac{Q_{ox}}{C_{ox}} \quad (1-15)$$

It is the gate-source potential that causes no band bending in the silicon.

MOST Threshold Voltage

- 3) The surface potential at the source side of the channel under strong inversion is $2\Phi_F$ (PHI in SPICE).
It's value is obtained from the distance between the Fermi level (in the bulk) and the middle of the energy bandgap of the semiconductor material. It also represents the band bending in strong inversion:

$$\Phi_F = \pm \frac{kT}{q} \ln \frac{N_{sub}}{n_i} \quad (1-16)$$

+ for nMOST and - for pMOST.

So Φ_F is a measure of the doping level, as well as conductivity.

MOST Threshold Voltage

- 4) The depletion charge Q_D which depends on the depletion layer thickness t_{si}

$$Q_D = qN_B t_{si} \Rightarrow \pm \frac{Q_D}{C_{ox}} = \pm \frac{qN_B}{C_{ox}} \sqrt{\frac{2\epsilon_{si}(\Phi_j - V_{BS})}{qN_B}} = \pm \frac{\sqrt{2\epsilon_{si}qN_B(\Phi_j - V_{BS})}}{C_{ox}} \quad (1-17)$$

$$\therefore \pm \frac{Q_D}{C_{ox}} = \pm \gamma \sqrt{(\Phi_j - V_{BS})} \cong \pm \gamma \sqrt{2|\Phi_F|} \quad \text{Note: built-in junction potential } \Phi_j \cong 2|\Phi_F|$$

for ($V_{BS} = 0$)

$$\Rightarrow \pm \frac{Q_D}{C_{ox}} = \pm \gamma \sqrt{2|\Phi_F| - V_{BS}} \quad (1-18)$$

Note: V_{BS} is negative such that V_{BS} and $2|\Phi_F|$ add up!
 V_T is then as follows:

$$V_T = V_{T0} \pm \gamma (\sqrt{2|\Phi_F| \mp V_{BS}} - \sqrt{2|\Phi_F|}) \quad (1-19)$$

γ M_T represents the body effect (or the effect of parasitic JFET)

Deviation of I/V Characteristics

Consider a semiconductor bar carrying a current I . if the charge density along the direction of current is Q_d coulombs per meter and the velocity of charge is v meters per second then:

$$I = Q_d \cdot v \quad (1-20)$$

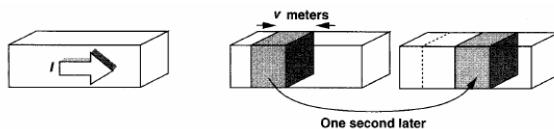


Fig 1.7
Semiconductor bar

Deviation of I/V Characteristics

Now consider an NFET whose source and drain are connected to ground (Fig 1.8a). The inversion charge density produced by the gate oxide cap. is proportional to $V_{GS} - V_T$. For $V_{GS} \geq V_T$, any charge placed on the gate must be mirrored by the charge in the channel, yielding a uniform channel charge density equal to:

$$Q_d = WC_{ox}(V_{GS} - V_T) \quad (1-21)$$

Total capacitance per unit length

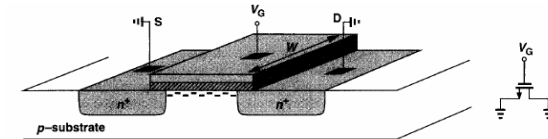


Fig 1.8a
Channel charge (equal source and drain voltage)

Deviation of I/V Characteristics

Now suppose that the drain voltage is greater than zero (Fig 1.8b). The local voltage difference between gate and channel varies from V_{GS} to $V_{GS} - V_D$ along the channel is:

$$Q_d(x) = WC_{ox}(V_{GS} - V(x) - V_T) \quad (1-22)$$

Where $V(x)$ is the channel potential at x

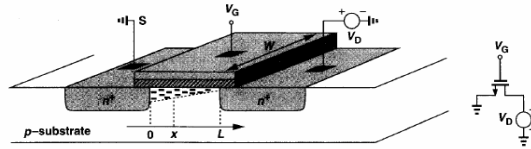


Fig 1.8 b
Channel charge (unequal source and drain voltage)

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Deviation of I/V Characteristics

From (1-20) the current is given by:

$$I_D = -WC_{ox}(V_{GS} - V(x) - V_T) \cdot v \quad (1-23)$$

$$v = -\mu_n \frac{dV(x)}{dx} \quad (1-24)$$

$$\Rightarrow I_D = -WC_{ox}(V_{GS} - V(x) - V_T) \mu_n \frac{dV(x)}{dx} \quad (1-25)$$

Considering the boundary conditions $V(0) = 0; V(L) = V_{DS}$ we obtain:

$$\int_{x=0}^L I_D dx = \int_{V=0}^{V_{DS}} WC_{ox} \mu_n (V_{GS} - V(x) - V_T) dV \quad (1-26)$$

$$I_D = \mu_n C_{ox} \frac{W}{L} \left[(V_{GS} - V_T) V_{DS} - \frac{1}{2} V_{DS}^2 \right] \quad (1-27)$$

Note: L is the effective channel length

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Deviation of I/V Characteristics

Regarding (1-27)

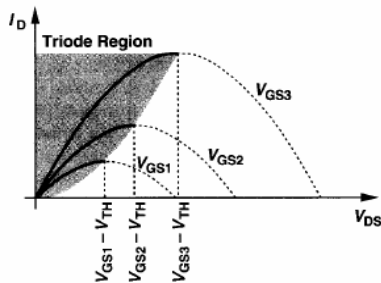


Fig 1.9
Drain current versus Drain-source voltage
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Deviation of I/V Characteristics

If in (1-27), $V_{DS} \ll 2(V_{GS} - V_T)$ then:

$$I_D \approx \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_T) V_{DS} \quad (1-28)$$

$$\Rightarrow R_{on} = \frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{GS} - V_T)} \quad (1-29)$$

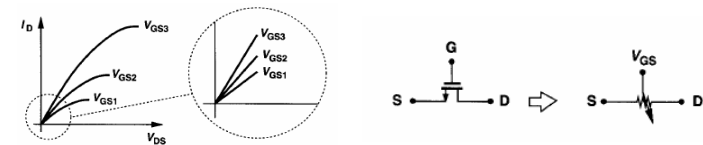


Fig 1.10
Linear operation in deep triode region
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Deviation of I/V Characteristics

In reality the drain current does not follow the parabolic behavior for (Fig 1.11), and becomes relatively constant (saturation region)

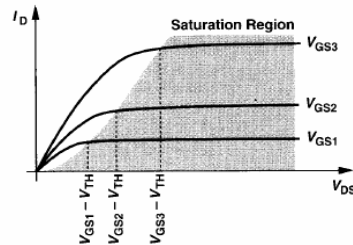


Fig 1.11

Linear operation in deep triode region

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Deviation of I/V Characteristics

The density of inversion layer charge is proportional to $V(x) - V_T$. So if $V(x)$ approaches V_T , then $V_{GS} - V_T$ drops to zero (Pinch-off). As V_{DS} increases further, the point at which $V(x)$ equals zero gradually moves toward the source (Fig 1.12). Now reconsidering (1-26) with $x = 0$ to $x = L_{pinch-off}$ and $V(x) = 0$ to $V(x) = V_{GS} - V_T$ we come to:

$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L_{pinch-off}} (V_{GS} - V_T)^2 \approx \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_T)^2 \quad (1-30)$$

Almost independent of drain-source voltage

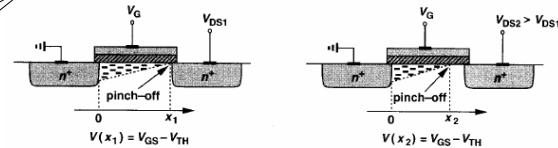


Fig 1.12

Pinch-off behavior

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Deviation of I/V Characteristics

Since a MOSFET operating in saturation produces a current in response to its gate-source overdrive voltage, we can define **Transconductance** to define how well the device converts voltage to current. *Transconductance* is denoted by and expressed as g_m

$$g_m = \left. \frac{\partial I_D}{\partial V_{GS}} \right|_{V_{DS}=cte} = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_T) \quad (1-31)$$

Transconductance represents the sensitivity of the device. it can be shown that:

$$g_m = \sqrt{2 \mu_n C_{ox} \frac{W}{L} I_D} \quad (1-32)$$

$$= \frac{2 I_D}{V_{GS} - V_T} \quad (1-33)$$

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Deviation of I/V Characteristics

Fig 1.13 shows g_m behavior

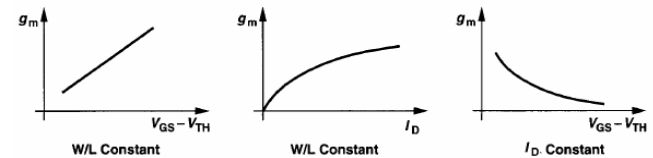


Fig 1.13

MOS transconductance as a function of overdrive and drain current

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Deviation of I/V Characteristics

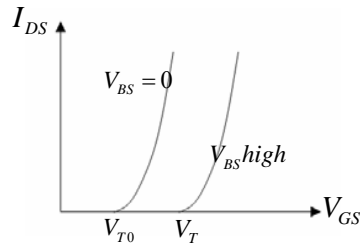


Fig 1.14
Plot of I_{DS} versus V_{GS} & V_{BS}

$$I_{DS} - sat = \frac{kp}{2n} \frac{W}{L} (V_{GS} - V_T)^2 \approx \frac{kp}{2n} \frac{W}{L} (V_{DS} - sat)^2 \quad (1-34)$$

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Deviation of I/V Characteristics

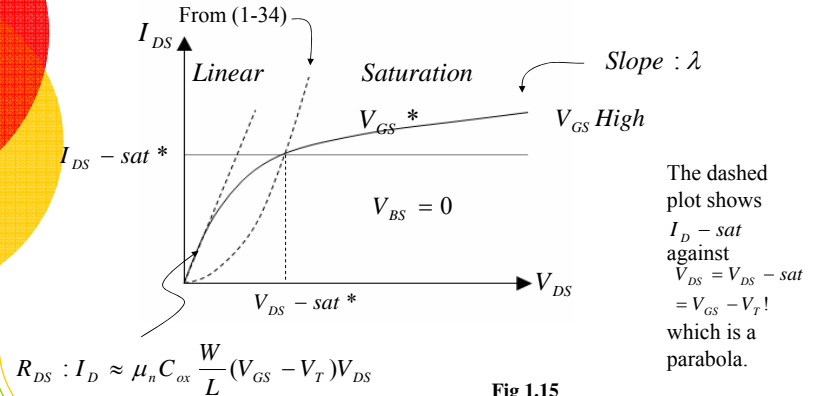


Fig 1.15
Plot of I_{DS} versus V_{GS} & V_{DS}

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Channel Length Modulation

As V_{DS} increases beyond $V_{DS} - sat$ as a result of the extension of the depletion layer charge at the drain into the channel toward the source (Fig 1.16) over a distance ΔL , the current is slightly increased. The voltage drop over ΔL is about $V_{DS} - sat$, so the channel is reduced over a distance from L to $L - \Delta L$. This can be represented as follows:

$$I_{DS-sat} = \frac{kp}{2n} \frac{W}{L} (V_{GS} - V_T)^2 (1 + \lambda (V_{DS} - V_{DS-sat})) \quad (1-35)$$

Unit: $1/V$

Parameter λ depends on L (inversely).
LAMBDA in SPICE

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Channel Length Modulation

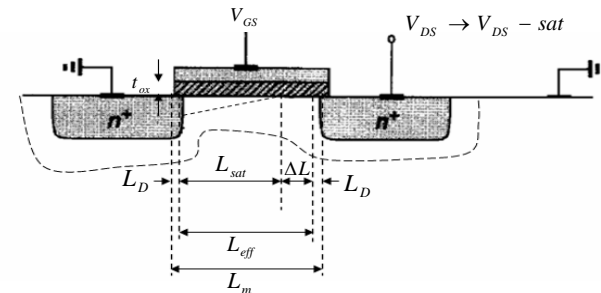


Fig 1.16
Channel length modulation

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Channel Length Modulation

Effective channel length and width

The effective channel length L_{eff} given by

$$L_{eff} = L_m - 2L_D - \Delta L \quad (1-36)$$

Where L_m is the channel length drawn in the layout (on mask)
 L_D is the under diffusion and
 ΔL is a reduction because of photolithography and etching

Similarly

$$W_{eff} = W_m + \Delta W \quad (1-37)$$

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Channel Length Modulation

Remember from (1-31):

$$\begin{aligned} g_m &= \frac{\partial I_D}{\partial V_{GS}} \big|_{V_{DS}=cte} \\ &= \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_T) = 2 \frac{k_p}{2n} \frac{W}{L} (V_{GS} - V_T) \\ &= \sqrt{2 \mu_n C_{ox} \frac{W}{L} I_D} = 2 \sqrt{\frac{k_p}{2n} \frac{W}{L} I_D} \\ &= \frac{2I_D}{V_{GS} - V_T} \end{aligned}$$

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Small signal parameters

Bulk transconductance g_{mb}

From (1-30) and (1-19):

$$\begin{aligned} I_{DS} &= \frac{k_p}{2n} \frac{W}{L} (V_{GS} - V_T)^2 = \frac{k_p}{2n} \frac{W}{L} (V_{GS} - [V_{T0} + \gamma(\sqrt{2|\Phi_F| - V_{BS}} - \sqrt{2|\Phi_F|})])^2 \\ g_{mb} &= \frac{\partial I_{DS}}{\partial V_{BS}} = \frac{\partial I_{DS}}{\partial V_T} \cdot \frac{\partial V_T}{\partial V_{BS}} \end{aligned}$$

Recall

$$\gamma = \frac{\sqrt{2\varepsilon_{si}qN_{SUB}}}{C_{ox}}$$

$$n - 1 = \frac{\gamma}{2\sqrt{\Phi_j - V_{BS}}} = \frac{1}{C_{ox}} \sqrt{\frac{\varepsilon_{si}qN_{SUB}}{2(\Phi_j - V_{BS})}}$$

so γ is independent of V_{BS} and
 n is dependent on V_{BS}

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Small signal parameters

$$\begin{aligned} \Rightarrow g_{mb} &= -2 \frac{k_p}{2n} \frac{W}{L} (V_{GS} - V_T) \cdot \frac{\partial V_T}{\partial V_{BS}} \\ &= -g_m \cdot \frac{\partial V_T}{\partial V_{BS}} = -g_m \left(-\gamma \cdot \frac{1}{2} \frac{1}{\sqrt{2|\Phi_F| - V_{BS}}} \right) \\ &= \frac{\gamma}{2\sqrt{2|\Phi_F| - V_{BS}}} \cdot g_m \quad (1-38) \end{aligned}$$

$$\text{From (1-11)} \quad g_{mb} = \frac{C_{BSQ}}{C_{ox}} g_m = (n - 1) g_m \quad (1-39)$$

$$\Rightarrow n = 1 + \frac{g_{mb}}{g_m} \quad (1-40)$$

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Small signal parameters

Note: g_{mb} represents the transconductance from the bulk input-node voltage to the output current. It is actually the transconductance of the parasitic JFET.

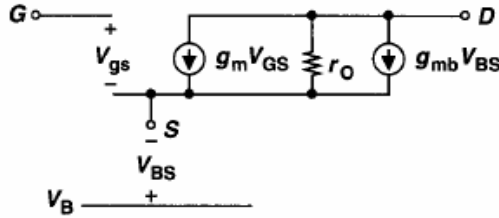


Fig 1.17

Small signal model

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Small signal parameters

Output Resistance r_o

It is the result of the channel-shortening effect by (channel length modulation).

$$g_o = \frac{\partial I_{DS}}{\partial V_{DS}} \approx \lambda I_{DSat} \quad (1-41)$$

$$\Rightarrow r_o = \frac{1}{\lambda I_{DSat}} \approx \lambda I_{DSat} \quad (1-42)$$

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Small signal parameters

$$I_{DS} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_T)^2$$

Using Taylor approximation:

$$\begin{aligned} I_{DS} &= I_{DS-sat} + \left[\frac{\partial I_{DS}}{\partial V_{DS}} \cdot \frac{\partial L_{eff}}{\partial V_{DS}} \right] \Delta V_{DS} \\ \Rightarrow I_{DS} &= I_{DS-sat} + \left\{ \frac{-\mu_n C_{ox} W}{2L_{eff}^2} (V_{GS} - V_T)^2 \right\} \cdot \left\{ \frac{\partial L_{eff}}{\partial V_{DS}} \right\} \cdot (V_{DS} - V_{eff}) \\ L_{eff} &= L - \Delta L = L - \sqrt{\frac{2k_{si} \epsilon_0}{qN_{SUB}}} \sqrt{\Phi_0 + V_{DS} - V_{eff}} = K_{DS} \sqrt{\Phi_0 + V_{DS} - V_{eff}} \\ \Rightarrow \frac{\partial L_{eff}}{\partial V_{DS}} &= \frac{-K_{DS}}{2\sqrt{\Phi_0 + V_{DS} - V_{eff}}} \\ \Rightarrow I_{DS} &= I_{DS-sat} \left(1 + \frac{K_{DS}}{2L\sqrt{\Phi_0 + V_{DS} - V_{eff}}} \cdot V_{DS} - V_{eff} \right) \quad (1-43) \end{aligned}$$

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$$\Rightarrow I_{DS} = I_{DS-sat} (1 + \lambda (V_{DS} - V_{eff})) \quad (1-44)$$

where :

$$\begin{aligned} \lambda &= \frac{K_{DS}}{2L\sqrt{\Phi_0 + V_{DS} - V_{eff}}} \\ r_o &= \frac{1}{\lambda I_{DS}} = \frac{2L\sqrt{\Phi_0 + V_{DS} - V_{eff}}}{K_{DS} I_{DS}} = \frac{2L}{I_{DS}} \sqrt{\frac{qN_A}{2\epsilon_{si}}} (\Phi_0 + V_{DS} - V_{eff}) \quad (1-45) \end{aligned}$$

Note: $r_o \propto (L, \sqrt{V_{DS}})$

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Small signal parameters

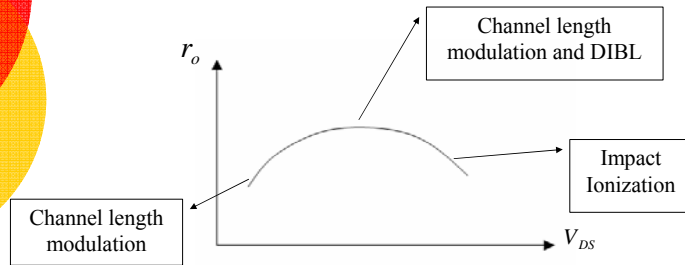


Fig 1.18

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Small signal parameters

Parameter λ depends on the channel length L , yet assumed to be constant in spice. therefore another is chosen, taking into account the dependence on channel length L :

Equation (1-42) can be rewritten as follows:

$$r_o = \frac{1}{g_{ds}} = \frac{V_E \cdot L}{I_{Dsat}} \quad (1-46)$$

Comparing (1-42) and (1-46) :

$$V_E = \frac{1}{\lambda L} = \frac{V_A}{L} \quad (1-47)$$

$$\Rightarrow V_E = \frac{2\sqrt{(V_{DS} - V_{eff} + \Phi_0)}}{K_{DS}} \quad (1-48)$$

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Small signal parameters

V_E is the Early voltage per unit-channel length. in analogy with the Early voltage of a Bipolar transistor. It is different for nMOST and pMOST for the difference in substrate doping level:

Note: Early voltage is independent of L

More doping level, the less extension of the depletion layer in to the channel \Rightarrow the larger substrate doping, the larger the Early voltage.

Example:

N-well CMOS process:

For the same channel length, the output resistance of the nMOST is thus smaller than o the pMOST, in an n-well CMOS process.

It is opposite for a p-well CMOS process:

$$V_{Ep} = 4V/\mu m L, V_{En} = 7V/\mu m L$$

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Small signal parameters

Another point of view:

$$I_D = \frac{k'}{2} \frac{W}{L} (V_{GS} - V_T)^2 \quad L_{eff} = L - X_d$$

$$\Rightarrow I_D = \frac{k'}{2} \frac{W}{L_{eff}} (V_{GS} - V_T)^2$$

$$\frac{\partial I_D}{\partial V_{DS}} = -\frac{k'}{2} \frac{W}{L_{eff}^2} (V_{GS} - V_T)^2 \cdot \frac{dL_{eff}}{dV_{DS}} = \frac{I_D}{L_{eff}} \cdot \frac{dX_d}{dV_{DS}} \quad (1-48)$$

So Early voltage is defined analogous to BJT

$$V_A = \frac{I_D}{\left(\frac{\partial I_D}{\partial V_{DS}}\right)} = L_{eff} \left(\frac{dX_d}{dV_{DS}}\right)^{-1} = \frac{1}{\lambda} \leftrightarrow \lambda = \frac{\left(\frac{dX_d}{dV_{DS}}\right)}{L_{eff}} \quad (1-49)$$

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Small signal parameters

$$V_E = \frac{1}{\lambda L_{eff}} = \frac{1}{\left(\frac{dX_d}{dV_{DS}}\right)} \quad (1-50)$$

$$X_d = \sqrt{\frac{2k_s \epsilon_0}{qN_A}} \sqrt{(\Phi_0 + V_{DS} - V_{eff})} \quad (1-51)$$

$$\Rightarrow \frac{dX_d}{dV_{DS}} = \frac{K_{DS}}{2\sqrt{\Phi_0 + V_{DS} - V_{eff}}} \quad (1-52)$$

$$\Rightarrow \lambda = \frac{\left(\frac{dX_d}{dV_{DS}}\right)}{L} = \frac{K_{DS}}{2L\sqrt{\Phi_0 + V_{DS} - V_{eff}}} \quad (1-53)$$

$$V_E = \frac{1}{\lambda L} = \frac{2\sqrt{\Phi_0 + V_{DS} - V_{eff}}}{K_{DS}} \quad (1-53)$$

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Small signal parameters

$$r_o^{-1} = \frac{\partial I_D}{\partial V_{DS}} = \frac{I_D}{L_{eff}} \frac{dX_d}{dV_{DS}} = \frac{I_D}{L_{eff}} \frac{K_{DS}}{2\sqrt{\Phi_0 + V_{DS} - V_{eff}}} \quad (1-54)$$

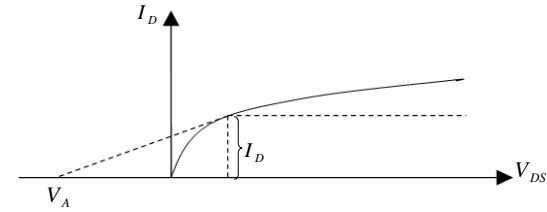


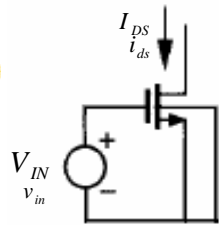
Fig 1.19
Early Voltage

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Small signal analysis examples

Example 1



$$V_{T0} = 0.7 \text{ V}$$

$$\gamma = 0.86 \text{ V}^{1/2}$$

$$n = 1.49 (V_{BS} = 0)$$

$$k = \mu_n C_{ox} = 30 \mu\text{A/V}^2 = k_p / 2n$$

$$\text{for } V_{IN} = 1.4 \text{ V}, \frac{W}{L} = \frac{50}{5}, v_{in} = 10 \text{ mV}_{rms}$$

$$\Rightarrow I_{DS}, i_{ds}, g_m, g_{mb}, r_o = ?$$

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Small signal analysis examples

$$(1-30) \quad I_{out} = \frac{k_p}{2n} \frac{W}{L} (V_{GS} - V_T)^2 = 30 \times \frac{50}{5} (1.4 - 0.7)^2 = 0.147 \text{ mA}$$

$$(1-31) \quad g_m = 2 \left(\frac{k_p}{2n}\right) \frac{W}{L} (V_{GS} - V_T) = 2 \times 30 \times \frac{50}{5} (1.4 - 0.7) = 0.42 \text{ mS (Simens)}$$

$$(1-38) \quad g_{mb} = \frac{\gamma}{2\sqrt{2\Phi_F - V_{BSQ}}} g_m = \frac{0.86}{2\sqrt{2\Phi_F}} \times 0.42 = 0.206 \text{ mS}$$

$$\text{Note that } 2\Phi_F = 0.684 \text{ V}$$

$$\text{for } v_{in} = 10 \text{ mV}_{rms} \Rightarrow I_{out} = g_m v_{in} = 4.2 \text{ mA}_{rms} \rightarrow 4.2\sqrt{2} = 5.94 \mu\text{A}$$

$$\text{for n-well process: } V_{En} = 4 \text{ V} / \mu\text{mL} \Rightarrow V_{En} \cdot L = (4 \text{ V} / \mu\text{mL}) \times 5 \mu\text{m} = 20 \text{ V}$$

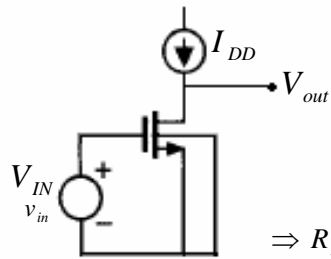
$$\Rightarrow r_o = \frac{V_{En} \cdot L}{I_{out}} = \frac{20}{0.147 \text{ mA}} = 136 \text{ k}\Omega$$

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Small signal analysis examples

Example 2: Amp with active load



$$\begin{aligned}
 V_{T0} &= 0.7\text{V} \\
 \gamma &= 0.86\text{V}^{1/2} \\
 n &= 1.49 (V_{BS} = 0) \\
 k &= 30 \mu\text{A/V}^2 \\
 \text{if } V_{DD} &= 8\text{V} \\
 \Rightarrow R_L &= ? \quad \text{for } V_{out} = 8/2 = 4\text{V}
 \end{aligned}$$

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Small signal analysis examples

$$R_L = \frac{V_{out}}{I_{DS}} = \frac{4}{0.15\text{mA}} = 27.2\text{k}\Omega$$

$$\Rightarrow R_L' = R_L \parallel r_o = 27.2 \parallel 136 = 22.7\text{k}\Omega$$

$$A_v = -g_m R_L' = -0.42\text{mS} \times 22.7\text{k}\Omega = -9.5\text{V/V}$$

from (1-33) and (1-46)

$$A_v = -g_m R_L = -\frac{2I_{DS}}{V_{GS} - V_T} \cdot \frac{V_{En} L}{I_{DS}} = -\frac{2V_{En} L}{V_{GS} - V_T} \quad (1-55)$$

The voltage gain is set by V_{GS} and L only (in strong inversion)

For high gain $V_{GS} - V_T$ must be chosen smallest possible (0.2V) and L as large as possible.

$$L = 10 \mu\text{m} \Rightarrow |A_v| = \frac{2 \times 4\text{V} / \mu\text{m} L \times 10}{0.2} = 400\text{V/V} \rightarrow 52\text{dB}$$

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Small signal analysis examples

Determine W : The larger W , The larger g_m and the smaller r_o
for $W = 5 \mu\text{m}$

$$\Rightarrow \begin{cases} I_{DS} = 6 \mu\text{A}, g_m = 60\text{mS} \\ r_o = 6.7\text{M}\Omega \end{cases}$$

Note: Do not increase I_D than necessary (for power consideration)

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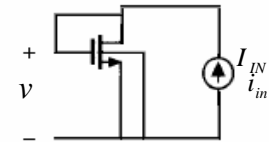
Small signal analysis examples

Example of MOST Diode

$$V_{GS} = V_{DS} \Rightarrow V_{DS} > V_{GS} - V_T$$

Always in saturation

There is no conduction for negative values so it is said to be a diode.

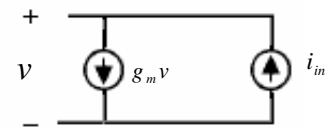


$$\text{for source grounded: } V_{GS} = V_T + \sqrt{\frac{I_{D-sat}}{k' W/L}}$$

Used for DC-shifter in MOS.

Voltage set by I and W/L .

AC voltage: i_{in} / g_m



AC resistance is $1/g_m$ (normally k_n is shunted by k_p) \Rightarrow still

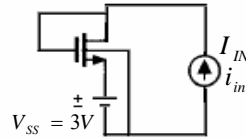
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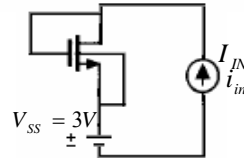
Small signal analysis examples

If using a voltage source:

if source is not grounded V_B must be included for V_T calculation (1-10), so increasing V_{GS} . But g_m is not changed since is constant, (1-30), (1-31) and (1-32)!



For p-well process →



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Small signal analysis examples

Example (No Body Effect)

$$V_{T0} = 0.7V, \gamma = 0.86V^{1/2}, n = 1.49 (V_{BS} = 0)$$

$$k' = 30 \mu A/V^2, \frac{W}{L} = 50$$

$$\Rightarrow V_{DS} = V_{GS} = ? \text{ for } I_{in} = 0.2mA, AC_{swing} : 10\%$$

$$\Delta V = V_{DS} = V_{GS} = 0.7 + \sqrt{\frac{0.2mA}{30 \times 10^{-6} \times 10}} = 0.7 + \sqrt{0.667} \approx 1.52V$$

$$g_m = \frac{2I_{DSQ}}{V_{GS} - V_T} = 2\sqrt{k' \frac{W}{L} I_{DSQ}} = 2\sqrt{30 \times 10^{-6} \times 10 \times 0.2mA} = 0.49mS$$

$$\Rightarrow \frac{1}{g_m} = 2.04k\Omega$$

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Small signal analysis examples

10% AC current:

$$I_{AC} = 0.10 \times (0.2mA) = 0.02mA$$

$$= g_m v_{in} \Rightarrow v_{in} = \frac{0.02mA}{0.49mS} = 40.8mV_p = 29mV_{rms}$$

Example (With Body Effect)

$$\text{for } V_S = 3V \Rightarrow V_T = 0.7 + 0.86(\sqrt{0.6 + 3} - \sqrt{0.6}) = 1.66V$$

$$\Rightarrow \Delta V = V_{GS} = 1.66 + \sqrt{0.667} = 2.48V$$

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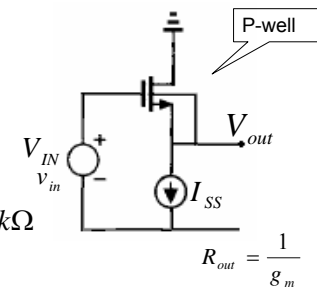
Small signal analysis examples

Examples of Source follower

I_{SS} is constant so V_{GS} must be constant too:

$$V_{in} - V_{out} = V_{GS} \longrightarrow \boxed{AC + DC}$$

$$\text{Gate is @ AC ground} \Rightarrow R_{out} = \frac{1}{g_m} = 2.04k\Omega$$



$$R_{out} = \frac{1}{g_m}$$

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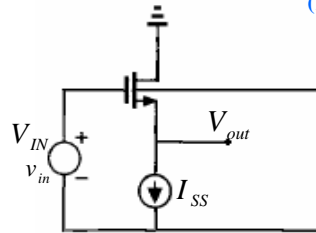
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Small signal parameters

For ground bulk:

$$V_{out} = V_{in} - V_{T0} - \gamma(\sqrt{2|\Phi_F| + V_{out}} - \sqrt{2|\Phi_F|}) - \sqrt{\frac{I_{SS}}{k'W/L}} \quad (1-56)$$

As it can be seen from (1-56) the gain is not unity! This is the result of the bulk effect or parasitic JFET.



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Small signal parameters

We can draw the parasitic JFET explicitly (Drain and source are common with MOST but its gate i.e. bulk is grounded.).

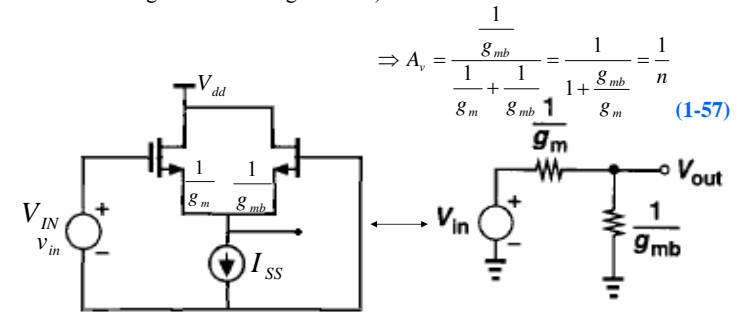


Fig 1.20a,b
Parasitic JFET

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$$\Rightarrow A_v = \frac{\frac{1}{g_{mb}}}{\frac{1}{g_m} + \frac{1}{g_{mb}}} = \frac{1}{1 + \frac{g_{mb}}{g_m}} = \frac{1}{n} \quad (1-57)$$

Small signal parameters

Description: Consider the MOS T-Model (Fig 1.21)

Note that since $i_s = g_m v_{gs}$ passes through $r_s = \frac{1}{g_{mb}}$, so the current into gate (G terminal) is zero, thereby input impedance is infinity!

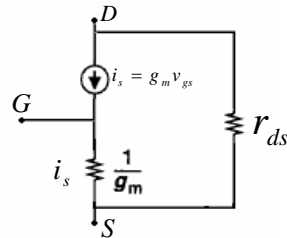


Fig 1.21
MOS T-Model

So the AC small signal model of the circuit is really as shown in Fig 1.20b. Also the model is shown in Fig 1.22 (without r_{ds})

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Small signal parameters

Note: If $V_{in} = 0 \Rightarrow V_{gs} = 0$ for $V_{in} \neq 0$ we can calculate V_s as a voltage divider of $1/g_m$ and $1/g_{mb}$, or according to T-Model we know that in any case is as follows (Fig 1.21):

$$i_s = g_m v_{gs} \Rightarrow v_o = v_s = \frac{g_m v_{gs}}{g_{mb}} = \frac{g_m (v_{in} - v_o)}{g_{mb}} \quad (1-58)$$

$$\Rightarrow v_o \left(1 + \frac{g_m}{g_{mb}}\right) = \frac{g_m v_{in}}{g_{mb}} \Rightarrow A_v = \frac{\frac{1}{g_{mb}}}{\frac{1}{g_m} + \frac{1}{g_{mb}}} = \frac{1}{1 + \frac{g_{mb}}{g_m}} = \frac{1}{n} \quad (1-59)$$

See(1-40)

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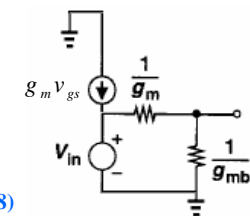


Fig 1.22

As shown
before in
(1.57)

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Small signal parameters

$$R_{out} = \frac{1}{g_m + g_{mb} + g_o} \approx \frac{1}{g_m + g_{mb}} \quad (1-60)$$

So bulk effect reduces gain and increases the V_{DS} ! It should be noted although we draw both Voltage source, and current source, in T-Model in Fig 1.22 the current going through is always $1/g_m$ as shown in Fig 1.21.

Example of MOST as a switch

Resistive Load

$$\frac{V_{out}}{V_{in}} = \frac{R_L}{R_L + R_{DS}}$$

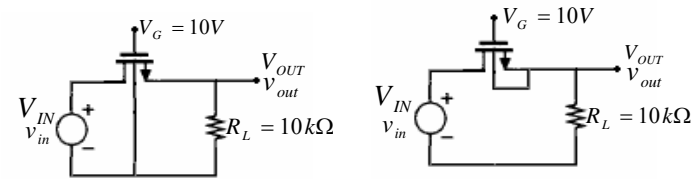


Fig 1.23a,b
MOST as switch with resistive load

Example of MOST as a switch

We are in Triode region:

$$r_{ds} = \frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{GS} - V_T - V_{DS})} \quad (1-61)$$

From (1-10):

$$R_{DS} = \frac{1}{\beta [V_G - V_{out} - V_{T0} - \gamma(\sqrt{2|\Phi_F| + V_{out}} - \sqrt{2|\Phi_F|})]} \quad (1-62)$$

where $\beta = \mu_n C_{ox} \frac{W}{L}$

Since V_G is large R_{DS} is small, so $V_{out} \approx V_{in}$

Example of MOST as a switch

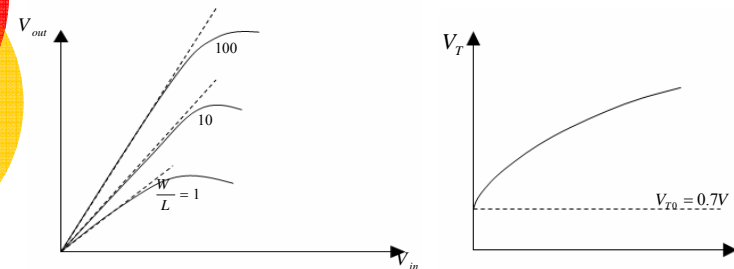


Fig 1.24a,b

Example of MOST as a switch

- The larger the transistor, the smaller the resistance.
- The lower the input voltage, The smaller the resistance
- The value of threshold voltage increases with input voltage as shown in Fig 1.24b.(for $V_{BS} \neq 0$ due to body effect)

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Example of MOST as a switch

Capacitive Load

Used in switched capacitor and CMOS logics.

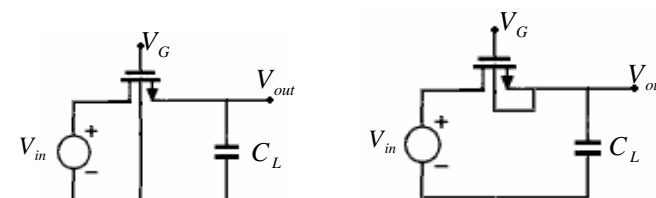


Fig 1.24a,b
MOST as switch with capacitive load

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Example of MOST as a switch

$$V_{IN} = 1.4V, \frac{W}{L} = \frac{50}{5}, v_{in} = 10mV_{rms}$$

for

$$\Rightarrow I_{DS}, i_{ds}, g_m, g_{mb}, r_o = ?$$

(1-54)

Fig 1.19

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MOS Transistor as a switch

Symbol



On Characteristics of a MOS Switch

Assume operation active region ($V_{DS} < V_{GS} - V_{TH}$ and V_{DS} is small).
Thus:

$$R_{ON} = \frac{V_{DS}}{i_D} = \frac{1}{\mu C_{ox} \left(\frac{W}{L}\right) (V_{GS} - V_{TH})}$$

OFF Characteristics of a MOS Switch

If $V_{GS} < V_{TH}$, then $i_D = I_{OFF} = 0$ when $V_{DS} \approx 0$.

If $V_{DS} > 0$, then:

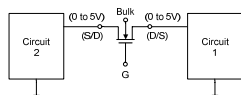
$$R_{ON} = \frac{1}{\lambda i_D} = \frac{1}{\lambda I_{OFF}} \approx \infty$$

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MOS Switch Voltage Range

If a MOS switch is used to connect two circuits that can have analog signal that vary from 0 to 5V, what must be the value of the bulk and gate voltages for the switch to work properly?



- To insure that the bulk-source and bulk-drain pn junction are reverse biased, the bulk voltage must be less than the minimum analog signal for a NMOS switch.
- To insure that switch is ON, the gate voltage must be greater than the analog signal pulse the threshold for a NMOS switch.

Therefore: $V_{\text{Bulk}} \leq 0V$
and $V_G > 5V + V_{\text{TH}}$
Also, $V_G(\text{OFF}) \leq 0V$

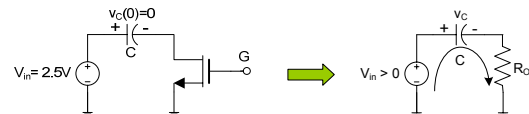
Unfortunately, the large value of reverse bias bulk voltage causes the threshold voltage to increase.

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Influence of the ON Resistance on MOS Switches

Finite ON Resistance:



Example:

Initially assume the capacitor is uncharged. If $V_G(\text{ON})$ is 5V and is high for 0.1μs, find the W/L of the MOSFET switch that will charge a capacitance of 10pF in five time constants

$$(K'_N = \mu_n C_{\text{ox}} = 110 \mu\text{A}/\text{V}^2 \text{ and } V_{\text{TN}} = 0.7 \text{ V})$$

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Influence of the ON Resistance on MOS Switches

Solution:

The time constant must be equal to $\frac{100 \text{ ns}}{5} = 20 \text{ ns}$ Therefore R_{ON} must be less than $\frac{20 \text{ ns}}{10 \text{ pF}} = 2 \text{ k}\Omega$

The ON resistance of the MOSFET (for small V_{DS}) is:

$$R_{\text{ON}} = \frac{1}{K'_N (W/L)(V_{\text{GS}} - V_{\text{TH}})} \Rightarrow \frac{W}{L} = \frac{1}{R_{\text{ON}} K'_N (V_{\text{GS}} - V_{\text{TH}})} = \frac{1}{2 \text{ k}\Omega \cdot 110 \mu\text{A}/\text{V}^2 \cdot 4.3} = 1.06$$

Comments:

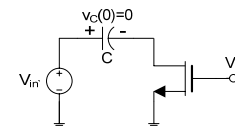
- It is relatively easy to charge on-chip capacitors with minimum size switches.
- Switch resistance is really not constant during switching and the problem is more complex than above.

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Including The Influence of the Varying ON Resistance

Gate-Source Constant:



$$g_{\text{ON}}(t) = K' \left(\frac{W}{L} \right) [(V_{\text{GS}}(t) - V_{\text{TH}}) - V_{\text{DS}}(t)]$$

$$g_{\text{ON-avg}} = \frac{1}{\tau_{\text{ON-avg}}} = \frac{g_{\text{ON}}(0) + g_{\text{ON}}(\infty)}{2}$$

$$V_{\text{DS}}(\infty) = 0, V_{\text{GS}}(0) = V_{\text{GS}}(\infty) = V_{\text{GS}}$$

$$g_{\text{ON-avg}} = \frac{K'}{2} \left(\frac{W}{L} \right) (V_{\text{GS}} - V_{\text{TH}}) - \frac{K'}{2} \left(\frac{W}{L} \right) V_{\text{DS}}(0) + \frac{K'}{2} \left(\frac{W}{L} \right) (V_{\text{GS}} - V_{\text{TH}})$$

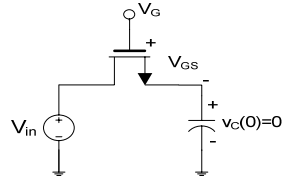
$$= K' \left(\frac{W}{L} \right) (V_{\text{GS}} - V_{\text{TH}}) - \frac{K'}{2} \left(\frac{W}{L} \right) V_{\text{DS}}(0)$$

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Including The Influence of the Varying ON Resistance

Gate-Source Constant:



$$g_{ON}(t) = K' \left(\frac{W}{L} \right) [(V_{GS}(t) - V_{TH}) - V_{DS}(t)]$$

$$g_{ON-avr} = \frac{1}{t_{ON-avr}} = \frac{g_{ON}(0) + g_{ON}(\infty)}{2}$$

$$g_{ON-avr} = \frac{K'}{2} \left(\frac{W}{L} \right) (V_{GS}(0) - V_{TH}) - \frac{K'}{2} \left(\frac{W}{L} \right) V_{DS}(0) + \frac{K'}{2} \left(\frac{W}{L} \right) (V_{GS}(\infty) - V_{IN} - V_{TH})$$

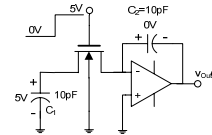
$$V_{DS}(\infty) = 0 = V_{GS}(\infty), V_{GS}(0) = V_{DD}$$

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Switch ON Resistance Example

Assume that at $t=0$, the gate of the switch shown is taken to 5V. Design the W/L value of the switch to discharge the C_1 capacitor to within 1% of its initial charge in 10ns. Use the MOSFET parameter for previous example.



Solution:

Note that the source of the NMOS is on the right and is always at ground potential so there is no bulk effect as long as the voltage across C_1 is positive. The voltage across C_1 can be expressed as:

$$v_{C1} = 5 \exp\left(\frac{-t}{R_{ON} C_1}\right)$$

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Switch ON Resistance Example

At 10ns, v_{C1} is 5/100 or 0.05V, therefore:

$$0.05 = 5 \exp\left(\frac{-10^{-8}}{R_{ON} 10^{-11}}\right) = 5 \exp\left(\frac{-10^3}{R_{ON}}\right) \Rightarrow \exp(G_{ON} 10^3) = 100$$

$$\Rightarrow G_{ON} = \frac{\ln(100)}{10^3} = 0.0046S$$

Note that the ON resistance is time variant:

$$G_{ON} = K' \frac{W}{L} [V_{DG}(t) - V_{TH}], \begin{cases} V_{DG}(0) = V_{DD} - 5V = 0 \\ V_{DG}(\infty) = V_{DD} - 0V = 5 \end{cases}$$

$$\therefore 0.0046 = K' \frac{W}{L} (V_{GS} - V_{TH}) - \frac{K'}{2} \frac{W}{L} V_{DS} = \left(110 \times 10^{-6} \cdot 4.3 - \frac{110 \times 10^{-6} \cdot 5}{2} \right) \frac{W}{L}$$

$$= 198 \times 10^{-6} \frac{W}{L} \Rightarrow \frac{W}{L} = \frac{0.0046}{198 \times 10^{-6}} = 23.2 \approx 23$$

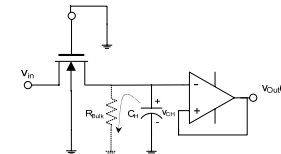
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Influence of The OFF State ON Switches

The OFF state influence is primarily in any current that flows from the switch to ground.

An example might be:



Typically, no problems occur unless capacitance voltages are held for a long time. For example:

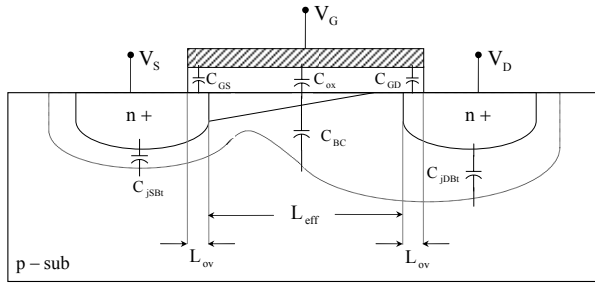
$$v_{out}(t) = v_{CH} \left[1 - e^{-t/(R_{Bulk} C_H)} \right]$$

If $R_{Bulk} \approx 10^9 \Omega$ and $C_H = 10 \text{ pF}$, the time constant is $10^9 \cdot 10^{-11} = 0.01 \text{ s}$.

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MOS Capacitances



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MOS Capacitances

$$C_{\text{ox}} = C_{\text{ox}} \cdot W \cdot L_{\text{eff}}$$

$$C_{\text{ox}} = \frac{\epsilon_{\text{ox}}}{t_{\text{ox}}}$$

Oxide (isolation) Cap.

t stands for total

$$C_{\text{BCt}} = C_{\text{jBC}} \cdot W \cdot L_{\text{eff}}$$

$$C_{\text{jBC}} = \frac{C_j}{\left(1 - \frac{V_{\text{BC}}}{\phi_j}\right)^{m_j}}, \quad \text{Depletion Region Cap. (junction Cap.)}$$

$$\phi_j = \phi_0 = V_T \ln \left(\frac{N_A N_D}{n_i^2} \right)$$

ϕ_j is the built-in potential of an open circuit pn junction. (PB)

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MOS Capacitances

$$C_{\text{jSBt}} = A_S \cdot C_{\text{jSB}} + P_S \cdot C_{\text{jswSB}}$$

$$C_{\text{jSB}} = \frac{C_j}{\left(1 - \frac{V_{\text{BS}}}{\phi_j}\right)^{m_j}}, \quad C_{\text{jswSB}} = \frac{C_{\text{jswSB}}}{\left(1 - \frac{V_{\text{BS}}}{\phi_{\text{jsw}}}\right)^{m_{\text{jsw}}}}$$

$$C_{\text{jDBt}} = A_D \cdot C_{\text{jDB}} + P_D \cdot C_{\text{jswDB}}$$

$$C_{\text{jDB}} = \frac{C_j}{\left(1 - \frac{V_{\text{BD}}}{\phi_j}\right)^{m_j}}, \quad C_{\text{jswDB}} = \frac{C_{\text{jswDB}}}{\left(1 - \frac{V_{\text{BD}}}{\phi_{\text{jsw}}}\right)^{m_{\text{jsw}}}}$$

$$C_{\text{jsw}} = \frac{\epsilon_{\text{si}}}{t_{\text{si}}} = \left(\frac{\epsilon_{\text{si}} q N_B}{2 \phi_{\text{jsw}}} \right)^{1/2}, \quad t_{\text{si}} = \text{Thickness of Depletion Layer}$$

$$m_j = m_{\text{jsw}} = 1/3, \dots, 1/2$$

A_S is the Source area, and P_S is the Source perimeter.

A_D is the Drain area, and P_D is the Drain perimeter.

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MOS Capacitances

In Saturation Region

$$C_{\text{GS}} = C_{\text{GSoV}} + 2/3 C_{\text{ox}}$$

$$C_{\text{GD}} = C_{\text{GDov}}$$

$$C_{\text{SB}} = C_{\text{jSBt}} + 2/3 C_{\text{BCt}}$$

$$C_{\text{DB}} = C_{\text{jDBt}}$$

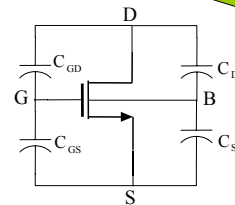
Overlap Capacitance between Gate and Source

Overlap Capacitance between Gate and Drain

Channel-Bulk junction Capacitance

Source-Bulk junction Capacitance

Drain-Bulk junction Capacitance



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MOS Capacitances

- In Triode (linear) Region**

$$\begin{aligned}C_{GS} &= C_{GDov} + 1/2 C_{oxl} \\C_{GD} &= C_{GDov} + 1/2 C_{oxl} \\C_{SB} &= C_{jSBt} + 1/2 C_{BCt} \\C_{DB} &= C_{jDBt} + 1/2 C_{BCt}\end{aligned}$$

